
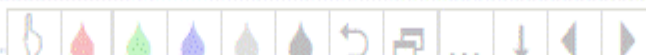


## Announcements – Lecture VII – Tuesday, Feb 13<sup>th</sup>

1. Exam 1: Saturday, February 24<sup>th</sup>, ISB 155/160 (General Chemistry Labs)  
Session I: 1:00-2:55, Last Name, A-J  
Session II: 3:00-4:55, Last Name, K-Z

2. Quiz 2: Place in basket.

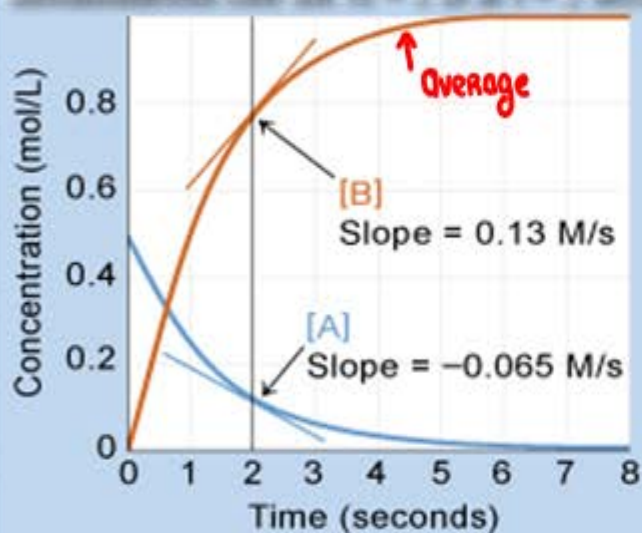
3. iClicker:  Pick any letter a-e



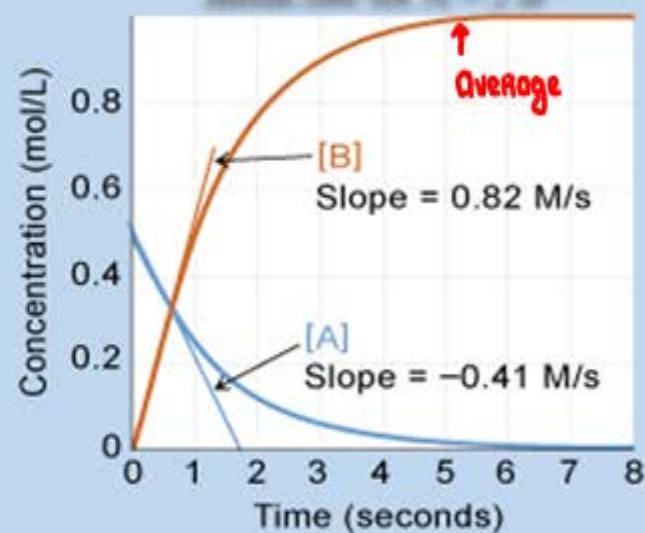
## 14.2 Expressing the Rate of a Reaction

### Instantaneous and Initial Rates

Instantaneous rate for  $A = 2 B$  at  $t = 2$  seconds



Initial rate for  $A = 2 B$



Initial rates are where the rate of formation and the rate of disappearance is fine.

Thus this is our region of choice.

## 14.3 Rate Laws

### Concentration and Reaction Rate

It should come as NO surprise that the rate of formation or disappearance is directly proportional to the concentration.



$$\text{Initial Reaction Rate} = k[A]^x[B]^y$$

$x$ : is referred to as the order with respect to A.

$y$ : is referred to as the order with respect to B.

$x + y$ : is the overall order of the reaction.

$k$ : is the rate constant.

**NOTE:**  $x$  and  $y$  are not necessarily equal to  $a$  and  $b$ .  
 $x$  and  $y$  can only be determined experimentally.

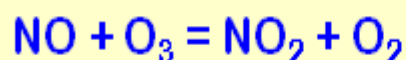
**NOTE:** Our discussion will initially be confined to orders: 0, 1 and 2.

For A: Zero order : Rate =  $k[A]^0$   
First order : Rate =  $k[A]^1$   
Second order : Rate =  $k[A]^2$



## 14.3 Rate Laws

### Determining Rate Law Using the Method of Initial Rates



- What is the rate law?
- What is the rate constant?

Exp	[NO] <sub>0</sub> , M	[O <sub>3</sub> ] <sub>0</sub> , M	Initial Rate, Ms <sup>-1</sup>
1	0.139	0.0436	0.527
2	0.139	0.0872	1.05
3	0.278	0.0436	1.05
4	0.278	0.0872	2.11

$$\begin{aligned} \text{Exp 1} \quad \text{Rate}_1 &= k [\text{NO}]_1^x [\text{O}_3]_1^y \\ 0.527 &= k (0.139)^x (0.0436)^y \end{aligned}$$

$$\begin{aligned} \text{Exp 2.} \quad \text{Rate}_2 &= k [\text{NO}]_2^x [\text{O}_3]_2^y \\ 1.05 &= k (0.139)^x (0.0872)^y \end{aligned}$$

$$\frac{\text{Rate}_2}{\text{Rate}_1} : \frac{1.05}{0.527} = \frac{k (0.139)^x (0.0872)^y}{k (0.139)^x (0.0436)^y}$$

$$\begin{aligned} 1.99 &= 2^y \\ y &= 1 \end{aligned}$$

$$\text{Exp 1.} \quad 0.527 = k (0.139)^x (0.0436)^y$$

$$\begin{aligned} \text{Exp 3} \quad \text{Rate}_3 &= k [\text{NO}]_3^x [\text{O}_3]_3^y \\ 1.05 &= k (0.278)^x (0.0436)^y \end{aligned}$$

$$\frac{\text{Rate}_3}{\text{Rate}_1} : \frac{1.05}{0.527} = \frac{k (0.278)^x (0.0436)^y}{k (0.139)^x (0.0436)^y}$$

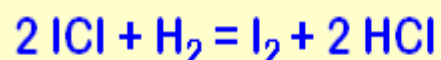
$$\begin{aligned} 1.99 &= 2^x \quad : \quad x = 1 \\ \text{Rate} &= k [\text{NO}] [\text{O}_3] \end{aligned}$$

$$\begin{aligned} \text{Exp 1 :} \quad 0.527 &= k (0.139) (0.0436) \\ k &= 86.9 \text{ M}^{-1} \text{ s}^{-1} \end{aligned}$$



## 14.3 Rate Laws

### Determining Rate Law Using the Method of Initial Rates



a) What is the overall order of the reaction **3**.

Exp	[ICl] <sub>0</sub> , M	[H <sub>2</sub> ] <sub>0</sub> , M	Initial Rate, Ms <sup>-1</sup>
1	0.309	0.114	7.07e-3
2	0.618	0.114	1.41e-2
3	0.309	0.228	2.83e-2
4	0.618	0.228	5.65e-2

Previously we did this the long way

this time we will do it the short way!

$$\text{Rate} = k [\text{ICl}]^x [\text{H}_2]^y$$

Exp 1 & 3: [ICl] is held constant while [H<sub>2</sub>] increases by a factor of 2.

Exp 1 & 2: [H<sub>2</sub>] is held constant while [ICl] increases by a factor of 2.

$$\frac{2.83 \times 10^{-2}}{7.07 \times 10^{-3}} = 4.00$$

$$2^y = 4$$
$$y = 2$$

$$\frac{1.41 \times 10^{-2}}{7.07 \times 10^{-3}} = 1.99$$

$$2^x = 2$$
$$x = 1$$

Overall order:  $2 + 1 = 3$



## 14.4 Concentration Changes over Time

### Integrated Rate Laws

#### Integrated Rate Laws for Reactions of Type A → Products

Reaction Order	Rate Law	Integrated Rate Law
Zero order	rate = $k[A]^0 = k$	$[A]_t = [A]_0 - kt$
First order	* rate = $k[A]$	$\ln \frac{[A]_t}{[A]_0} = -kt$
Second order	rate = $k[A]^2$	$\frac{1}{[A]_t} = \frac{1}{[A]_0} + kt$

t: time

$[A]_0$ : initial concentration of A @ time = 0

$[A]_t$ : concentration of A @ time = t

A = Products

$$-\frac{\Delta[A]}{\Delta t} = k[A]$$

$$\frac{d[A]}{dt} = -k[A] \quad \dots \text{if } \Delta \text{ is very small.}$$

$$(\frac{1}{[A]})d[A] = -kdt$$

$$\int_{t=0}^{t=t} (\frac{1}{[A]})d[A] = -k \int_{t=0}^{t=t} dt$$

$$\ln [A]_t - \ln [A]_0 = -kt$$

$$\ln \frac{[A]_t}{[A]_0} = -kt$$

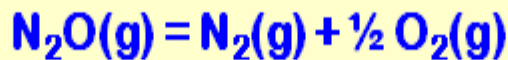


## 14.4 Concentration Changes over Time

### Integrated Rate Laws



The decomposition of nitrous oxide



is **second order in  $\text{N}_2\text{O}$**  with a rate constant of  $1.20 \times 10^{-3} \text{ M}^{-1}\text{s}^{-1}$ .

If the initial concentration of  **$\text{N}_2\text{O}$  is 1.79 M**, the concentration of  **$\text{N}_2\text{O}$  will be 0.187 M** after how many **seconds**.

~?,000 s

↳ 4

$$\frac{1}{[\text{A}]_t} = \frac{1}{[\text{A}]_0} + kt$$

$$[\text{A}]_0 = 1.79 \text{ M}$$

$$[\text{A}]_t = 0.187 \text{ M}$$

$$k = 1.20 \times 10^{-3} \text{ M}^{-1}\text{s}^{-1}$$

$$t = ?$$

$$\frac{1}{0.187} = \frac{1}{1.79} + 1.20 \times 10^{-3} t$$

$$5.348 = 0.5587 + 1.20 \times 10^{-3} t$$

$$1.20 \times 10^{-3} t = 5.348 - 0.5587$$

$$t = \frac{4.7893}{1.20 \times 10^{-3}} = 3,991 \text{ s}$$



## 14.4 Concentration Changes over Time

### Graphical Determination of Reaction Order

#### Determining the Rate Equation: Graphical Method

Description

The rate law for reactions involving a single reactant can be determined using the graphical method. This method involves constructing a series of plots of concentration vs. time data and analyzing the plots to extract the reaction order and the rate constant.

The general reaction used for this tutor is:



The concentration vs. time data at right were collected by running the reaction at a constant temperature. These are data taken for a single trial of the reaction.

Rate =  [A]

Submit

time, min	[A], mol/L	time, min	[A], mol/L
0	0.7245	5	0.4046
1	0.6605	6	0.3406
2	0.5965	7	0.2766
3	0.5325	8	0.2126
4	0.4686		



- [A] vs. Time
- ln[A] vs. Time
- 1/[A] vs. Time
- Least Squares

Plot

